

Connectivity-based Performance Evaluation for Mobile Cognitive Radio Network

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Abstract—In this paper, we propose a model of mobile cognitive radio network after fully considering the analysis method of network connectivity based on random way-point (RWP) mobility scheme. The closed-form solution of connectivity probability has been derived to evaluate the network performance in this model. And it shows that the network connectivity is related to the size of mobile cognitive radio network, the number of secondary users, the transmission range of secondary users and primary users, the interference range of secondary users and primary users, the number of primary users and the activity factor of primary users. Simulation results are good agreement with numerical results, which verifies our theoretical analysis is correct and reasonable.

Index Terms—mobile cognitive radio network, random way-point mobility model, network connectivity, connectivity probability

I. INTRODUCTION

Cognitive radio has emerged as a promising technology to enhance spectrum utilization by sensing the spectrum and opportunistically using the spectrum of primary users [1-4]. In cognitive radio network, there are two kinds of users: primary users (PUs) and secondary users (SUs). PUs are licensed users with high priority in the utilization of the spectrum, which constitute the primary network. SUs are unlicensed users with low priority in the utilization of the spectrum, which constitute the secondary network. It is important to understand the connectivity of the secondary network so that proper network operations can be performed. In traditional wireless ad hoc network, the communication among nodes is realized by using the same frequency. The distance between the transmitter and the receiver and the transmission power of the transmitter are the only parameters affecting the network connectivity. But in cognitive radio network, two SUs can connect if they are in radio visibility and have at least one available common channel. As a consequence, the node position, the transmission power and their free spectrum bands all affect cognitive radio network connectivity. In other words, the connectivity is the foundation of reliable data

transmission in cognitive radio network. A communication link exists between two SUs if the two SUs meet the following two conditions: (1) they are within each other's transmission range; (2) they have a common spectrum band determined by the transmitting and receiving activities of nearby PUs.

Several recent works have analyzed and proposed the methods for the network connectivity. Network connectivity of one-dimensional ad hoc network was studied in [5-7]. The movement of nodes with impact on the connectivity of ad hoc network was elaborated in [5]. In [8-9], the research method of ad hoc network connectivity has been applied to not only one-dimensional network but also two-dimensional network, the relationship between network parameters (e.g., transmitting range and node degree) and network connectivity was analyzed in detail. But the authors in [5-9] only studied connectivity of traditional ad hoc network without studying the cognitive radio network connectivity (CRNC). In [10-13], the CRNC based on the connectivity of graph was studied, and the second smallest eigenvalue of Laplacian matrix was used to denote the CRNC, the analysis method provides a methodology to evaluate the CRNC. However, the analysis method is only based on the static network topology with fully available topological information on SUs and PUs without considering the movement of SUs. In [14-18], percolation theory was used to analyze the CRNC, but it is only applicable to large scale cognitive radio network. Two basic properties of cognitive radio network [19], capacity and connectivity, were studied to characterize the relationship and tradeoff among key system parameters involved in these properties. Connectivity opportunity selection algorithm [20] was proposed to select the best connectivity alternative for the user in a heterogeneous wireless multi-hop network. In [21], connectivity-aware minimum-delay routing was discussed in vehicular ad-hoc networks. We can see from [19-21] the CRNC is very useful to the projecting and routing of network. As far as we know, the mobile CRNC has not been adequately analyzed so far.

In this paper, we propose the model of mobile cognitive radio network (MCRN) after the model of one-dimensional mobile ad hoc network in [5] gives us inspiration. Our model is very useful for certain applications such as BusNet in [22] where buses are mobile and bus stops are stationary. In this case, BusNet may be a secondary network which is composed of SUs. The PUs are some network devices. In other words, the developed model can be used to realize the communication among vehicle to vehicle along roads by using the unlicensed spectrum bands, which provides many applications (e.g., accident warning and traffic indication). It is noted that we only investigate CRNC and don't consider what protocol is used to realize communication in the paper.

With the proposed model, we firstly derive the closed formula of connectivity probability in MCRN, and then analyze the impact of network parameters on connectivity probability. Lastly we further verify that the theoretical analysis is reasonable through simulation.

The rest of the paper is organized as follows: In Section 2, we present the system model for evaluating the MCRN connectivity. Section 3 is dedicated to the analysis of connectivity based on the system model. Simulation results are reported in Section 4. Finally, we conclude the paper in Section 5.

II. SYSTEM MODEL

Consider a channel model with path loss and small scale fading governed by the propagation-related power attenuation model, $P_r = P_t |h|^2 d^{-\alpha}$, where P_r is the received power, P_t is the transmission power, d is the distance between the transmitter and receiver under consideration, $\alpha \geq 2$ is the path loss exponent and h represents the small scale fading component. Obviously, the distance between the transmitter and receiver is given by

$$d = \left(\frac{P_t |h|^2}{P_r} \right)^{1/\alpha} \tag{1}$$

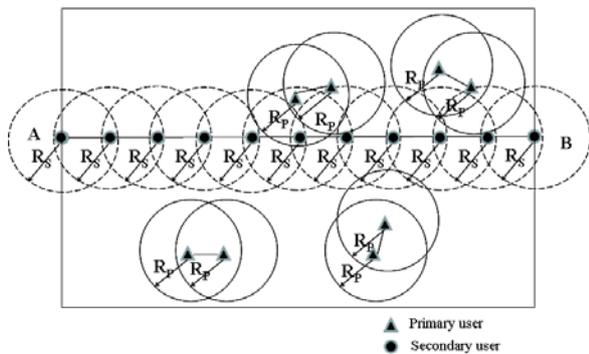


Figure 1. Model of mobile cognitive radio network.

The developed network model is illustrated in Fig. 1, we assume the MCRN is composed of N_s mobile SUs, stationary secondary source node A and destination node

B and N_p motionless PUs. We consider a road as a line in the model, and mobile SUs are uniformly placed along the line between A and B at the beginning. Then they move along the line between A and B based on RWP mobility model. The network size is represented with the length L and the width D which means the distance between A and B is L . PUs are uniformly distributed within the cognitive radio network region.

We assume PUs and SUs are equipped with omnidirectional antenna, denoting the primary transmission range with R_p and the secondary transmission range with R_s . The circle with radius R_p denotes the coverage area of the PU, and the circle with radius R_s denotes the coverage area of the SU. Now we investigate connectivity problem and only consider bidirectional links in the secondary network when we define connectivity. Therefore, when we determine whether there exists a communication link between two SUs, we need to check the existence of spectrum opportunities in both directions and the distance between these two nodes. The secondary network consists of all the SUs and all the bidirectional secondary links. As for primary network, we also consider that any primary link between two PUs is bidirectional, and a potential primary link exists between any two PUs if and only if the distance between these two nodes is less than the primary transmission range R_p , the primary links are illustrated in Fig. 1.

We assume that each $PU_j (j = 1, \dots, N_p)$ has a licensed spectrum band with carrier frequency f_j , denoted as channel ch_j , and all the PUs transmit with a given transmission power P , and each PU_j is characterized by an *on-off transmission* with activity factor β_j .

$$\beta_j = \frac{t_{ON}^j}{t_{ON}^j + t_{OFF}^j} \tag{2}$$

where t_{ON}^j and t_{OFF}^j are the average duration of the activity period of the PU and the average duration of silence period of the PU, respectively. In addition, let E_j represent the event that " PU_j does not transmit at an arbitrary time t ". Then the probability that this event happens is as follows.

$$P(E_j) = 1 - \beta_j \tag{3}$$

Each secondary user opportunistically exploits locally unused licensed spectrum without interfering transmissions of PUs. In the same time, let A_j represent the event that " PU_j transmits at an arbitrary time t " with probability of $P(A_j) = \beta_j$. Assuming that the events A_1, A_2, \dots, A_{N_p} are independent and unrelated. The probability that all the PUs are active (i.e., the probability that all the PUs transmit at the same time) is as follows.

$$p_{active} = P\left(\bigcap_{j=1}^{N_p} A_j\right) = \prod_{j=1}^{N_p} P(A_j) \tag{4}$$

Here we represent the interference region of a primary user as a dish of radius R_{p_i} and the interference region of a secondary user as a dish of radius R_{s_i} (see Fig. 2). So the behavior of a secondary link at any given time slot is dependent on two conditions: firstly, all active PUs are out of the two interference regions of the two associated SUs; secondly, these two SUs are out of the interference regions of all currently active PUs. Assuming that an active SU or PU may refer to either a transmitter or a receiver at a given time slot. Then the minimum distance between an active PU and an active SU is equal to $R_i = \max\{R_{p_i}, R_{s_i}\}$, which corresponds to the *maximum interference range*, as illustrated in Fig. 2 where $R_{p_i} > R_p$, $R_{s_i} > R_s$. To reflect the characteristic of the real wireless communication environment, we use the Log-Normal Shadowing Model [23] and assume $R_{p_i} = (6/5)R_p$ and $R_{s_i} = (6/5)R_s$. Notice that we define the interference region centered at some PU or SU with radius R_i as the *maximum interference region (MIR)*. Therefore, a SU_i can transmit by using channel ch_j in two different cases:

1) when the distance between PU_j and SU_i is longer than or equal to R_i , SU_i always identifies the channel ch_j as unused;

2) when the distance between PU_j and SU_i is shorter than R_i and PU_j is inactive.

If one of these two cases occurs, the channel ch_j is available for the SU_i .

According to the proposed network model, there are $N_s + 1$ segments to form the secondary network. For the convenience of connectivity analysis, additional terms are defined as follows:

X : A continuous random variable describing the location of a mobile cognitive node at any instant time, which represents the distribution of secondary nodes. The PDF and CDF of X are $f(x)$ and $F(x)$.

K_x : A random variable denoting the length of a segment with the left edge locating at x . The PDF and CDF of K_x are $q_x(k)$ and $Q_x(k)$, respectively.

L_i : A random variable denoting the location of the left edge of the i -th segment. Let $r_i(l)$ represent the PDF of L_i .

$p_{i,k}$: The probability that the i -th segment has a length shorter than or equal to k when all the PUs are inactive. In practical application, k is a constant representing the distance between the transmitter and the receiver. Assuming that R_s is equal to k throughout the paper.

$p_{i,k}^c$: The probability that the i -th segment has a length shorter than or equal to k when PUs located in the *MIR* of SU_{i-1} or SU_i are active and there is at least one common channel between SU_{i-1} and SU_i .

p_c : The connectivity probability of MCRN when PUs located in the *MIR* of any secondary user are inactive.

p_c^c : The connectivity probability of MCRN when PUs located in the *MIR* of any secondary user are active.

III. CONNECTIVITY ANALYSIS

In this section, we analyze connectivity of MCRN. If all the PUs located in the *MIR* of any secondary user are inactive, SUs always have available common channel. The network composed by SUs can be considered as a traditional one dimensional mobile ad hoc network. The link between two nodes is only influenced by the distance between two nodes. Now we review an existing conventional one dimensional mobile ad hoc network connectivity analysis [5].

$$q_x(k) = N_s [f(x+k)] [1 - (F(x+k) - F(x))]^{N_s - 1} \quad (5)$$

where $0 \leq x \leq L$ and $0 \leq k \leq L - x$. Obviously the CDF of K_x is as follows:

$$Q_x(k) = 1 - [1 - (F(x+k) - F(x))]^{N_s} \quad (6)$$

The left edge of the i -th segment will be located at l if one node is located at l , and the remaining $i - 2$ and $N_s - i + 1$ nodes are located on the left and right sides of the node located at l , respectively. Hence, the following equation can be obtained

$$r_i(l) = N_s [f(l)] C_{N_s - 1}^{i - 2} [F(l)]^{i - 2} [1 - F(l)]^{N_s - i + 1} \quad (7)$$

where $2 \leq i \leq N_s + 1$ and $0 \leq l \leq L$. From (5), (6), and (7), the probability that the i -th segment with its left edge located at x has a length shorter than or equal to k can be described as $Q_x(k) r_i(x)$. Then $p_{i,k}$ is defined as

$$p_{i,k} = \int_0^{L-k} Q_x(k) r_i(x) dx + \int_{L-k}^L r_i(x) dx \quad (8)$$

In (8), due to the border effect, when the left edge of a segment falls between $L - k$ and L , the segment is always shorter than k , indicating a connection, i.e. $Q_x(k) = 1$. Hence the connectivity probability in conventional one dimensional mobile ad hoc network when the above analysis is applied becomes the following:

$$p_c = \begin{cases} Q_0(k) \left(\prod_{i=2}^{N_s+1} p_{i,k} \right) & N_s \geq \left\lceil \frac{L}{k} \right\rceil - 1 \\ 0 & N_s < \left\lceil \frac{L}{k} \right\rceil - 1 \end{cases} \quad (9)$$

In practice, since some PUs are active, the topology of MCRN will be affected by active PUs, and SUs may interfere with communication of PUs when SUs apply the same frequency bands as the active PUs. So the connectivity analysis method of conventional mobile ad hoc network is inappropriate. For instance, when the distance of the i -th link between SU_{i-1} and SU_i is shorter

than or equal to k , the i -th segment is considered to be connected which means the i -th link is valid in conventional mobile ad hoc network. But the link may be invalid if there is no available channel between them in cognitive radio network. Hence, the analysis method described above must be revised.

In Fig. 2, one can see transmission range (R_s, R_p) and interference range (R_{SI}, R_{PI}) for SU and PU, respectively. To realize communication between SU_{i-1} and SU_i , we must consider behavior of PUs and choose channels which are not used by PUs. This implies that the SU_{i-1} (SU_i) can transmit data to SU_i (SU_{i-1}) if the transmission from SU_{i-1} (SU_i) does not interfere with nearby primary nodes. To solve the interference problem, we consider the minimum distance between an active primary user and an active secondary user is equal to $R_l = \max\{R_{PI}, R_{SI}\}$ when we analyze the network connectivity. We can see from Fig. 2 the channel of primary link 1 is always available to the link between SU_{i-1} and SU_i , the primary link 2 and the primary link 3 are not the case because of the relative location of PUs and SUs. There are two possible cases for the i -th secondary link which depend on the location of SU_{i-1} and SU_i . Let $R_l < x < L - R_l$ represent the first case of the *MIR* of SU_{i-1} or SU_i being completely within cognitive radio network region and $0 \leq x < R_l$ or $L - R_l \leq x \leq L$ corresponds to the other case which is the *MIR* of SU_{i-1} or SU_i being partly within cognitive radio network region.

For the case of $R_l < x < L - R_l$: Fig. 2 shows SU_{i-1} is located at $(x, 0)$, and the *MIR* centered at SU_{i-1} is indicated with $C_{i-1} = \pi R_l^2$. We denote PDF of PUs with $g_{wv}(w, v) = \frac{1}{D.L}$. The probability that a primary user is located within the scope of C_{i-1} is indicated with $p_{i-1}(x)$.

$$p_{i-1}(x) = \iint_{C_{i-1}} g_{wv}(w, v) dA = \frac{\pi R_l^2}{D.L} \quad (10)$$

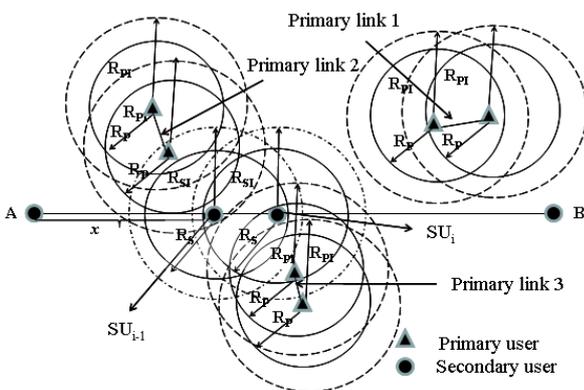


Figure 2. Link between two neighboring SUs under influence of PUs

Similarly, SU_i is located at $(x+k, 0)$, and the *MIR* centered at SU_i is indicated with $C_i = \pi R_l^2$. The probability that a primary user is located within C_i is denoted with $p_i(x+k)$.

$$p_i(x+k) = \iint_{C_i} g_{wv}(w, v) dA = \frac{\pi R_l^2}{D.L} \quad (11)$$

Overlapping area of the *MIR* which is covered by SU_{i-1} and SU_i is represented with C_{com}

$$C_{com} = R_l^2 \arccos \frac{k^2 - 2R_l^2}{2R_l^2} - k \sqrt{R_l^2 - \frac{k^2}{4}} \quad (12)$$

The probability that all the PUs are located in the *MIR* of SU_{i-1} or SU_i is denoted with p_{all-pu} and given by

$$p_{all-pu} = \begin{cases} \sum_{j=0}^{N_p} C_{N_p}^j [p_{i-1}(x)]^j [wp_i(x+k)]^{N_p-j}, & N_p \geq 1 \\ 0, & N_p = 0 \end{cases} \quad (13)$$

where, $w = (C_i - C_{com}) / C_i$. If all the PUs are located in the *MIR* of SU_{i-1} or SU_i , and all the PUs are active, the probability that there is no available common channel between SU_{i-1} and SU_i is given by

$$P_{nc} = p_{all-pu} P_{active} \quad (14)$$

For the case of $0 \leq x < R_l$ or $L - R_l \leq x \leq L$: This happens when not all the *MIR*s of SU_{i-1} or SU_i are located within cognitive radio network region. Notice that the probability that all the PUs are located in the *MIR* of SU_{i-1} or SU_i within cognitive radio network region is different from (13). Due to the symmetry of the model, the analysis method of $0 \leq x < R_l$ is the same as it of $L - R_l \leq x \leq L$, so we only analyze the case of $0 \leq x < R_l$ in the paper. The *MIR* which is covered by SU_{i-1} or SU_i within the scope of MCRN is denoted by $C_{b-total}$ and is given by

$$C_{b-total} = \frac{3}{2} \pi R_l^2 + k \sqrt{R_l^2 - \frac{k^2}{4}} - 2R_l^2 \arcsin \frac{\sqrt{R_l^2 - \frac{k^2}{4}}}{R_l} \quad (15)$$

The probability that all the PUs are located in the *MIR* of SU_{i-1} or SU_i within cognitive radio network region is p_{all-pu}^b and given by

$$p_{all-pu}^b = \begin{cases} \left(\frac{C_{b-total}}{D.L}\right)^{N_p}, & N_p \geq 1 \\ 0, & N_p = 0 \end{cases} \quad (16)$$

The probability that there is no common channel between SU_i and SU_{i-1} is P_{b-nc} and given by

$$p_{b-nc} = p_{all-pu}^b p_{active} \tag{17}$$

In MCRN, the link between two nearest neighboring secondary users relies on the distance and available common channel between them. If the two nodes are within the transmission range of each other and they have at least one available common channel, the link is valid, otherwise the link is noneffective. Therefore, the connectivity probability of the i -th segment between SU_{i-1} and SU_i is given by

$$\begin{aligned} p_{i,k}^c &= \beta_{b-nc} \int_0^{R_t} Q_x(k) r_i(x) dx \\ &+ \beta_{nc} \int_{R_t}^{L-R_t} Q_x(k) r_i(x) dx \\ &+ \beta_{b-nc} \int_{L-R_t}^{L-k} Q_x(k) r_i(x) dx \\ &+ \beta_{b-nc} \int_{L-k}^L r_i(x) dx \end{aligned} \tag{18}$$

where $\beta_{b-nc} = (1 - p_{b-nc})$ or $\beta_{nc} = (1 - p_{nc})$ is the probability that there is at least one available common channel between SU_{i-1} and SU_i for $0 \leq x < R_t$ and $L - R_t \leq x \leq L$ or $R_t < x < L - R_t$, respectively. The connectivity probability of MCRN is

$$p_c^c = \begin{cases} Q_0(k) \left(\prod_{i=2}^{N_s+1} p_{i,k}^c \right), & N_s \geq \left\lceil \frac{L}{k} \right\rceil - 1 \\ 0, & N_s < \left\lceil \frac{L}{k} \right\rceil - 1 \end{cases} \tag{19}$$

The steady-state mobile cognitive users distribution of the RWP mobility model is given in [24], and the PDF and CDF is shown as follows.

$$\begin{cases} f(x) = -\frac{6}{L^3}x^2 + \frac{6}{L^2}x, & 0 \leq x \leq L \\ F(x) = -\frac{2}{L^3}x^3 + \frac{3}{L^2}x^2, & 0 \leq x \leq L \end{cases} \tag{20}$$

Using above equations, the connectivity probability of mobile cognitive radio network can be calculated via numerical method.

IV. NUMERICAL RESULTS

Let us now verify these analytical results by computer simulation. In our simulation environment, SUs move according to the RWP model in a line, whose length and width have been set as $L = 1000m, D = 780m$, respectively. Each secondary user picks a random spot in a line and moves there with a constant speed which is randomly chosen in $[0, 5m/s]$. Upon reaching this point, the node randomly picks a new destination and repeats the process. The transmission range and interference range of the PUs, whose positions are assumed static, have been set to $R_p = 180m$ and $R_{pi} = 216m$, respectively. The interference range of SUs is related to transmission range R_s . We assume any mobile cognitive node will move towards the contrary direction at the same speed if

it reaches the border (i.e., A or B) during the sampling interval. Our simulation results are repeated 10000 times, 200 random network topologies are generated during simulation. Such the experiment is repeated 50 times for every network topology, and finally averaged over all 200 random network topologies (i.e., 10000 experiments).

Given $N_p = 7$ and the activity factor of primary users $\beta_j = 1 (j = 1, \dots, N_p)$, the resulting curves are shown in Fig. 3 and Fig. 4. It may be observed that this simulation yields the same qualitative behavior as the analytical plots.

In Fig. 3, it shows simulation results are in good agreement with theoretical results for $R_s = 0.15km, 0.18km, 0.2km$, respectively. As expected, in all the three cases, the value of p_c^c increases with increase of N_s for given R_s or with increase of transmission range R_s for given N_s . One can see from Fig. 3 that p_c^c is close to 1 when N_s is larger than 55 for fixed $R_s = 200m$. To reach some connectivity target p_c^c , the smaller the transmission range of SUs is, the more number of SUs in the secondary network is.

Fig. 4 gives the curve obtained with our formula and that produced by the simulations, we obtain the acceptable results between analytical and simulation results. Fig. 4 demonstrates that p_c^c increases with increase of transmission range R_s and the number of SUs. For fixed N_p , the relationship among p_c^c, N_s and R_s is similar to Fig. 3. Notice that an increase of the transmission power of some SU leads to an increase of interference with PUs and other SUs, and the energy consumption increases accordingly. So we should take the full consideration of the tradeoff between energy consumption and network connectivity.

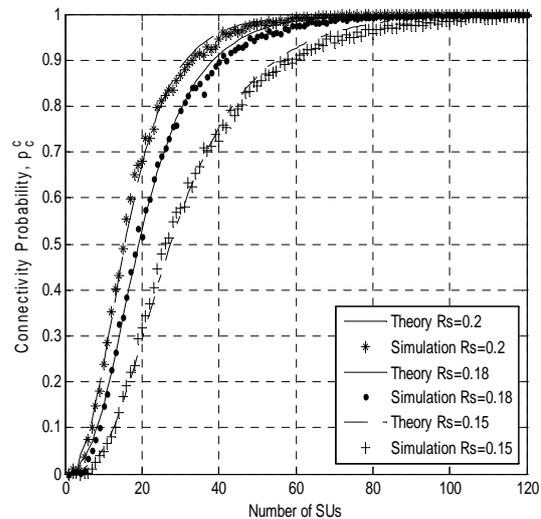


Figure 3. Analytical and simulation results for different R_s

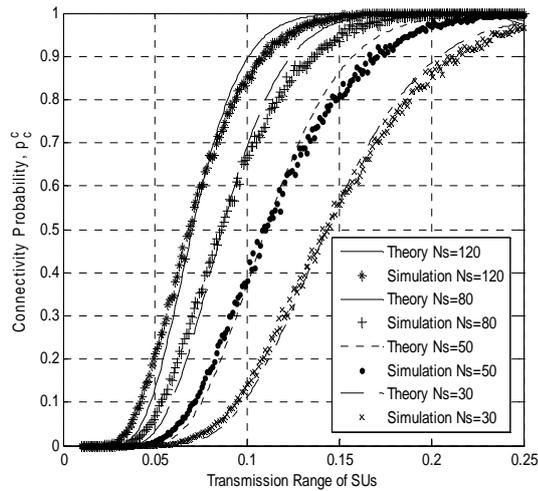


Figure 4. Analytical and simulation results for different N_s

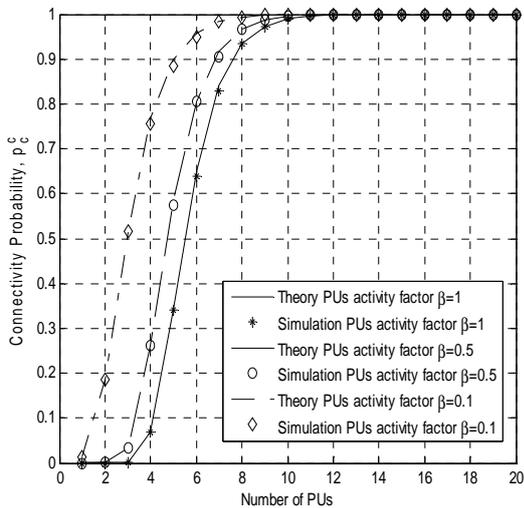


Figure 5. Number of PUs N_p versus connectivity probability P_c^c

Assuming $R_s = 0.15\text{km}$, $N_s = 80$, Fig. 5 gives the theoretical and simulation plots for different PUs activity factor $\beta_j = 1, \beta_j = 0.5, \beta_j = 0.1$ ($j = 1, \dots, N_p$), and simulation results further verify our analysis. One can see that the value of p_c^c increases with the increase of number of PUs for fixed PUs activity factor, but the p_c^c decreases with the increase of PUs activity factor β_j for fixed N_p . When the number of PUs is large enough, the connectivity performance of MCRN is close to that of conventional mobile ad hoc network. The larger the activity factor of PUs is, the worse the network connectivity becomes. This is so because the secondary network in our model is a linear network. Increasing the number of PUs or decreasing the activity factor of PUs implies increasing the probability of available common channel between any two neighbor cognitive users.

V. CONCLUSIONS

This paper investigated the connectivity of a MCRN with RWP mobility model. We proposed a network model and derived an analytical expression which was the closed form solution of connectivity probability. We pointed out that the connectivity probability was relevant to some parameters and showed that the connectivity of the cognitive radio network was greatly impacted by the number of the PUs, the activity factor of PUs, the number of the SUs, the transmission range of the SUs, the maximum interference range R_i . Besides, increasing the number of PUs is helpful to MCRN connectivity. A comparison is made between the theoretical analysis and simulation in various scenarios. The results derived in this paper are of practical value for researchers and developers who design MCRN or study routing of MCRN based on the connectivity probability.

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