Abstract—Harris corner detection algorithm called Harris corner detector is a very effective corner algorithm for gray-scale images. The corners extracted by Harris corner detector are stable, reliable, homogeneous and reasonable. However, it has own inevitable limitations. For the shape recognition of parts, an improved Harris corner detector is proposed in this paper. Based on the analysis of Harris corner detector, B-spline function is chosen as smooth filter instead of Gaussian function. And then the convolution template of B-spline function is provided. Some experiment results indicate that the improved Harris corner detector is effective and superior.

Index Terms—Shape recognition, Harris corner detector, smooth filter, Gaussian function, B-spline function, convolution template.

I. INTRODUCTION

With the rapid advance of industrial production automation, it is a trend for manufacture to improve the efficiency, intelligence and precision. In the process of production, machine vision has important applications such as the detection and recognition of machine parts, production monitoring[1]. What is more important, the human eye cannot meet the detection requirements in some industrial situation. Compared with the human eye, machine vision can improve significantly the production efficiency and automation level. In the meantime, machine vision can also save the labor cost. In recent years, with the development of image recognition, object detection has acquired a series of success in the video sequences and 2D images[1-5].

As an important branch of the machine vision, shape recognition is widely applied to in the fields of parts localization in industrial production, product quality testing and so on [4]. At present, the shape recognition methods of parts are based on the profile, the ratio of length to width and the degree of rectangle. Paijit K. suggest that humans can identify structured shapes by some interest points in local image[5]. Because interest points could represent visually information and are robust to partial occlusion, some researchers have applied interest points to recognize objects in various successful cases.

Corners are the local features of an image that can decide the shape of an object. So, it can be used widely in machine vision and pattern recognition. Harris corner detector is a method of corner extraction based on a gray-scale image[6]. It adopts a local autocorrelation function method that is robust to noise, rotation and lighting. However, it adopts Gaussian low-pass filter to smooth the gray-scale image. So it has some problems, such as the position offsets and the information lose of the corners. In addition, it's very poor real-time performance because of the large amount of calculation.

This paper proposes an improved Harris corner detector to recognize corner points in some part images. A B-spline function can converge to a Gaussian function. In additional, it has the characteristics of data fitting, low-pass flting, good approximation and compactness. So the Gaussian low-pass filter of Harris corner detector can be replaced with a B-spline function. In this paper, the improved Harris corner detector has two improvements: 1) using a B-spline filter to smooth noise before corner extraction; 2) establishing a window inhibition function to erase the pseudo corners after corner extraction.

II. HARRIS CORNER DETECTOR

Harris corner detector is a classic corner detection algorithm proposed by Harris C and Davis L S.A in 1988 [6]. Based on a local auto-correlation function, the basic
idea of Harris corner detector is to recognition a point by a small sliding window and to use a gradient formulation to detect response at any shift. If the point is a corner point, shifting the window in any direction can yield a large change in the intensity of the detect response. With characteristics of rotation invariance, scale invariance and high reliability, Harris operator is used to corner detection in a gray-scale image. The corner is proportional to the principal curvatures of the autocorrelation function that can represent the intensity change rate of the local image. So, Harris corner detector can be applied to detect the shape of parts in a gray-scale image by the differential operation and autocorrelation matrix. While shifting the small sliding window at any shift \((u, v)\) in any direction, the intensity change \(E(u, v)\) can be quantified by sum-of-squared difference (SSD).

\[
E(u, v) = \sum_{x,y} W_{x,y} [(I_{x+u,y+v} - I_{x,y})^2] \tag{1}
\]

Where \(W_{x,y}\) is a Gussian window function, \(I_{x,y}\) is the pixel intensity at the position \((x,y)\) in a gray-scale image, \(I_x = \partial I_{x,y} / \partial x\) and \(I_y = \partial I_{x,y} / \partial y\) which can be got by convoluting difference operator [7].

\[
I_x = I_{x,y} \otimes (-1, 0, 1) \tag{2}
\]
\[
I_y = I_{x,y} \otimes (-1, 0, 1)^T
\]

Where \(\otimes\) is the convolution operator, the first order gradient operator reflects the intensity change of the pixels in any direction, which can effectively distinguish between corner pixels and edge pixels, so Harris corner detector has rotation invariance. At the same time, Harris corner detector selects a Gaussian function as a detection window function, which can smoothly filter the image to well inhibit the noise.

Supposed gradient matrix \(M\) is the 2 by 2 symmetric matrix:

\[
M = \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} = [A \ C] [C \ B] \tag{3}
\]

Where \(A\), \(B\), and \(C\) can be calculated as following equations:

\[
A = I_x^2 \otimes w \tag{4}
\]
\[
B = I_y^2 \otimes w \tag{5}
\]
\[
C = (I_x I_y) \otimes w \tag{6}
\]
\[
w_{x,y} = \exp(-(x^2 + y^2) / 2\sigma^2) \tag{7}
\]

Where \(w_{x,y}\) is a smooth window function produced by the Gaussian function, and equations (1) can be expressed as:

\[
E(u, v) = Au^2 + 2Cuv + Bv^2 = [u \ v]M[u \ v]^T \tag{8}
\]

Because the sliding window auto-correlation function of a corner point has a minimum value when centered on the corner, gradient matrix \(M\) is used to detect corner points [4]. Supposing \(\lambda_1\) and \(\lambda_2\) are two eigenvalues of \(M\), if \(\lambda_1\) and \(\lambda_2\) both are high then the intensity change of \(E(u, v)\) is also tremendous, so the point is a corner. If one of \(\lambda_1\) and \(\lambda_2\) has big eigenvalue then the point situates the edge point. If \(\lambda_1\) and \(\lambda_2\) both are very small then the intensity change \(E(u, v)\) is very small in any direction. In order to avoid calculating the eigenvalues \((\lambda_1, \lambda_2)\) of matrix \(M\), Harris corner detector defines a corner response function \(G\) to detect corner points. Supposed that \(Det(M)\) is the determinant of the matrix \(M\) and \(Tr(M)\) is matrix trace of the matrix \(M\) [8], then

\[
Tr(M) = \lambda_1 + \lambda_2 = A + B \tag{9}
\]
\[
Det(M) = \lambda_1 \lambda_2 = AB - C^2 \tag{10}
\]
\[
G = Det(M) - k \cdot Tr(M)^2 \tag{11}
\]

Where \(k\) is an empirically determined constant and \(k = 0.04\) is proposed[6]. Then corner points can be selected by a given threshold to determine the minimum of \(G\). In other words, one point is considered as corner point only when its response value \(G\) is greater than the given threshold.

III. GAUSSIAN FUNCTION AND B-SPLINE FUNCTION

A. The Drawback of Gaussian Function

Using a Gaussian function to smooth a gray-scale image, there are two problems:

1. For a Gaussian function \(G(x) \in L^\infty(R)\), function \(f(x)\) would be excessively smoothed. Owing to \(g(x) = f(x) \otimes G(x)\), the better smoothness, the image smoothed is the worse compared with the original image. According to the differential property of the convolution operator:
\[ \frac{\partial^n}{\partial x^n} g(x) = \frac{\partial^n}{\partial x^n} [f(x) \cdot G(x)] \]

(12)

And

\[ G(x) \in L^\infty(R) \]

Thus

\[ g(x) \in L^\infty(R). \]

(2) Image smoothing mainly aims to improve the signal-to-noise ratio and eliminate noise. However, during the procedure of smoothing image using a Gaussian function, edge as high frequency components will be smoothed out. In addition, some edge will be transformed into graded and compressed on the image histogram. As a consequence, corner may be lost easily on the maximum inhibition. Harris corner detector has high stability, especially in L-shaped corner detection, but smoothing filter designed by the Gaussian function may cause image information loss for excessive smoothness. Above all, the Gaussian window’s size is not easy to control in the practical application. According to the consequence of the central limit theorem, a B-spline function can well approximate Gaussian function. So it is commonly used in computer vision [9]. Some researchers have presented a more general proof that B-spline function can converge to the Gaussian function in \( L^p(R), \forall p \in [2, +\infty) \) as the order \( n \) of the B-spline tends to infinity. Since the variance \( \sigma^2 \) of the B-spline function with \( n \) order is \( \frac{n+1}{12} \), the approximation relation is as follows.

\[ \beta^n(x) = \frac{1}{\sqrt{2\pi}\sigma^2} \exp\left(-\frac{x^2}{2\sigma^2}\right), \quad \sigma = \sqrt{\frac{n+1}{12}} \]

(15)

In Fig.1, the Gaussian function is drawn in a solid line and the cubic B-spline is drawn in a dotted line. From Fig.1, there is a graphical comparison between the Gaussian function and the cubic B-spline function. Besides, both the physiological and biological experiments [10] have shown that the human vision can be modeled with the Gaussian function. Thus, B-spline function is suitable for modeling biological vision because of their close approximation to the Gaussian function.

IV. IMPROVED HARRIS CORNER DETECTOR

A. B-spline Filter Operator

Compared with the Gaussian function, the order number \( n \) of the B-spline function is adjustable. So this paper adopts the B-spline function to improve Harris corner detector. With the increase of \( n \), the smooth performance is better. However, reducing the order \( n \) can enhance approximation performance [11].

The B-spline function with \( n \) order can be rewritten as follows.

\[ \beta^n(x) = \frac{6}{\pi(n+1)} \exp\left(-\frac{6x^2}{n+1}\right) \]

According to the consequence of the central limit theorem, a B-spline function can well approximate...
\[ B_n(x) = \sum_{j=0}^{n+1} \binom{n+1}{j} (-1)^j C_n^{j+1}(x + \frac{n+1}{2} - j)u(x + \frac{n+1}{2} - j) \]  
\[ u(x) = \begin{cases} 0, & x < 0 \\ 1, & x \geq 0 \end{cases} \quad (x \in \mathbb{R}) \]  
(16)

Where \( n \) usually could be set as 3. If \( n = 3 \), \( B_3(x) \) can be got as

\[ B_3(x) = \frac{1}{6} \begin{cases} 0, & \lvert x \rvert > 2 \\ (-\lvert x \rvert + 2)^3, & 1 < \lvert x \rvert \leq 2 \\ (-\lvert x \rvert + 2)^3 - 4(-\lvert x \rvert + 1)^3, & 0 < \lvert x \rvert \leq 1 \end{cases} \]  
(18)

When \( n \) increases, the smoothing effect become better and filter ability gets stronger, but the processing time may be delayed and easy to lose the information of boundary. When \( n \) decreases, the approximation performance of function become well to protect the details, but ability of removing noise becomes weak.

The local discrete function of a two-dimensional B-spline function could be written as follows.

\[ \Psi(x, y) = \sum_{i}^{x+m} \sum_{j}^{y+n} f(i, j) B_{m \times n}(x-i, y-j) \]  
(19)

Where \( f(i, j) \) is gray-scale value of the pixel at the position \((i, j)\), \( B_{m \times n}(x-i, y-j) \) is B-spline filter templates. It is known that B-spline can be separable, so

\[ B_{mn}(x-i, y-j) = B_m(x-i)B_n(y-j). \]

Usually, the size of the filter templates \( B_{m \times n} \) is \((2m+1) \times (2n+1)\), thus

\[ m = l = n \]

If \( n = 3 \) then

\[ B_{3 \times 3} = \frac{1}{6} \begin{bmatrix} 1 & 4 & 1 \\ 4 & 16 & 4 \\ 1 & 4 & 1 \end{bmatrix} \]  
(20)

B. Differential Form of B-spline Function

The space of a square integral function contains the \( n \)th spline function which is the \( n \)th piecewise polynomial and has \((n-1)\)th derivative. According to the definition of Schoenberg [12], the two-dimensional of the \( n \)th spline function can be expressed by

\[ V^n = \{ \varphi^n(x) = \sum_{k \in \mathbb{Z}} C(k) B^n(x-k) \} \quad (x \in \mathbb{R}, C \in L_2) \]  
(21)

where \( B^n(x) \) can be written by

\[ B^n(x) = \frac{(n+1-x)B^{n-1}(x+\frac{1}{2})+(n+1-x)B^{n-1}(x-\frac{1}{2})}{n} \]  
(22)

The two-dimensional form of above equation can expressed by

\[ g^n(x, y) = \sum C(k,l) B^n(x-k, y-l) \]  
(23)

And B-spline function is separable, so

\[ B^n(x-k, y-l) = B^n(x-k)B^n(y-l) \]  
(24)

The derivative of equation (21) and (22) can expressed by

\[ \frac{\partial g^n(x, y)}{\partial x} = \sum C(k,l) \frac{\partial B^n(x-k)}{\partial x} B^n(y-l) \]  
(25)

\[ \frac{\partial g^n(x, y)}{\partial y} = \sum C(k,l) B^n(x-k) \frac{\partial B^n(y-l)}{\partial y} \]  
(26)

Moreover, using equation (22), equation (27) can be derived.

\[ \frac{\partial B^n(x)}{\partial x} = B_{n-1}(x+\frac{1}{2}) - B_{n-1}(x-\frac{1}{2}) \]  
(27)

Combined equation(27) and equation(26), the first rank differential templates of B-spine function can be figured out, namely, the first-order differential filter template in \( x \) direction (smoothing filtering in \( y \) direction) can expressed by

\[ m_x = \frac{1}{12} \begin{bmatrix} 1 & 4 & 1 \\ 0 & 0 & 0 \\ -1 & -4 & -1 \end{bmatrix} \]  
(28)

The first-order differential filter template in \( y \) direction (smoothing filtering in \( x \) direction) can be expressed by

\[ m_y = \frac{1}{12} \begin{bmatrix} 1 & 0 & -1 \\ 4 & 0 & -4 \\ 1 & 0 & -1 \end{bmatrix} \]  
(29)

The second-order differential filter template can be expressed by

\[ m_{xy}^2 = \frac{1}{12} \begin{bmatrix} 1 & 1 & 1 \\ 0 & -8 & 0 \\ 1 & 1 & 1 \end{bmatrix} \]  
(30)

C. Improved Corner Detection Algorithm

The procedures of improved Harris corner detector are as follows [13]:

1) Using B-spline filter dispose image, namely using B-spline filter template (equation(20)) to instead Gaussian function.
Using the differential operator of B-spline to calculate $I_x^2$ and $I_y^2$ in x and y direction of image,

$$
\begin{align*}
I_x^2 &= I_x \times I_x \\
I_y^2 &= I_y \times I_y \\
I_x I_y &= I_x \times I_y
\end{align*}
$$

(31)

3) Responsibly convolute $I_x^2$, $I_y^2$, $I_x I_y$ with B-spline filter, the value name still be named as $I_x^2$, $I_y^2$, $I_x I_y$, then get the matrix $M$ with four elements.

$$
M = \begin{bmatrix}
I_x^2 & I_x I_y \\
I_x I_y & I_y^2
\end{bmatrix}
$$

(32)

4) Calculating the intensity of each corner pixel, namely,

$$
D_{et}(M) = AB - C^2 = \lambda_1 \times \lambda_2
$$

(33)

$$
Tr(m) = A + B = \lambda_1 + \lambda_2
$$

(34)

$$
G = D_{et}(M) - k \times Tr^2(M), k = 0.04
$$

(35)

4) Finally, if $G$ is the local maximum within a neighborhood and is larger than the given threshold then the current point can be considered as a corner point.

In general, increasing the given threshold, the number of the corner points becomes less; Reducing the threshold, then the number of corner can be increased. In addition, the size of local maximum neighborhood may influence the quantity and tolerance of the improved Harris corner detector.

V. PART SHAPE RECOGNITION PROCESS

A. The Composition of the Image RECOGNITION System

An image recognition system can be divided into four main units, and it’s block diagram is shown as Fig.2.

The first unit is the image information acquisition, which includes survey and comprehends of the object to acquire the most basic information. Image recognition system digitalizes the analog images acquired by camera equipment, and then input them into computer for subsequent processing.

The second unit is image preprocessing. The purpose of the preprocessing is to remove background noise, enhance image, meanwhile convert the original image into a form which is suitable for computer to feature extraction. It includes image transform, enhancement and so on.

The third unit is the image feature extraction. Based on the image processing, based on the analysis and summary, here can highlight the characteristics of the object. What feature parameters selected is of relating to identify the object.

The fourth unit is the image matching. Namely according to the feature parameters extracted, the paper uses some classification discriminators and rules to classify image characteristics, so as to get recognition result.

Parts shape recognition is a real-time image processing system based on computer [14]. Its working procedures are as follow:

1) Collecting the part shape image
2) Preprocessing the part shape image acquired and extract image features such as corners
3) Analyzing the similarity between the part shape image acquired and its template image
4) Matching shape.
Fig. 3 shows the flow of parts shape recognition algorithm. Firstly, collecting parts image by camera. Secondly, using computer software to process the image including gray level transformation, filtering, de-noising and so on. Thirdly, extracting corners and removing pseudo corners for obtaining shape features. Finally, matching image.

Collecting image data: Fig. 4 shows that how to use a digital array to represent a physical image in the process of collecting imagery by camera. Physical image is divided into small blocks called image elements (picture elements) or pixels [15].

Gray-scale conversion: System reads image data and manages pixel by its own function. Generally the color image acquired in RGB color space could convert to gray-scale image as follows.

\[ I = \frac{(R + G + B)}{3} \]  

B-spline filtering: because the order of the B-spline function is adjustable, the B-spline filter deposes image without appearing the negative effect brought from the little wave truncation. Meanwhile, the B-spline filter has very high filtering efficiency utilizing fast Fourier transformation. So this paper chooses the discrete B-spline convolution template \( B_{3 \times 3} \) to smooth the parts shape image.

Corner extraction: Similar to Harris algorithm, if both \( \lambda_1 \) and \( \lambda_2 \) are large enough, the corresponding pixel is recognized and extracted as a corner. Assumed that threshold is \( R \), a point is the corner if \( G \) is larger than \( R \).

Removing pseudo corner: it can be removed by the strategy of joining adjacent point, choosing a \( 3 \times 3 \) template sliding on the whole image. If there is more than one corner, the corner with the biggest \( G \) is retained by removing adjacent points out. This method could restrain the phenomenon of corner cluster.

Shape matching: Extracting the parts shape characteristic to establish library from the template images and matching corners extracted by inquiring characteristic library [16]. Here, the features extraction includes two aspects.

1) Giving priority to the number of corner points, for some simple shapes of parts such as the quadrilateral and triangular parts, using corner point number for identification.

2) Considering the relative position of corners, the number of part shape corner points extracted is consistent with its template.

After imagery sampling, there is only one part’s surface absorbed, where two-dimensional intensity image is only considered. Establishing library of common shape parts is good to comprise with angular point extracting.

Part shape recognition methods are shown in Table I.

VI. EXPERIMENT AND RESULT ANALYSIS

In this paper, parts shape recognition algorithm is realized by Matlab programming. The improved Harris corner detection algorithm is verified by square part, circular part and common tool such as hammer as examples shown as Fig. 5.

Fig. 6 shows the disposal results by improved Harris corner detection algorithm, Fig. 7 shows the disposal results by Harris corner detection algorithm and Fig. 8 is the disposal results after removing pseudo corner based on Fig. 6.

<table>
<thead>
<tr>
<th>TABLE 1</th>
<th>PART SHAPE RECOGNITION METHODS</th>
</tr>
</thead>
<tbody>
<tr>
<td>part shape</td>
<td>Polygon(cross-shape,d,T-shaped)</td>
</tr>
<tr>
<td>The number of corners</td>
<td>cross-shaped has 12, T-shaped has 8</td>
</tr>
<tr>
<td>Matching method</td>
<td>corner point number matching</td>
</tr>
</tbody>
</table>

Figure 4. Part’S images

Figure 5. Physical images and the Digital image

Figure 6. Comparison between improved algorithm with original algorithm
Compared Fig.6 with Fig.8, the improved Harris corner detector can obtain more corners and more accurate than the original Harris corner detector. The experimental results show that the improved Harris corner detector is superior to the original Harris corner detector in performance.

From Fig.6, 7, 8, the images of square part and circular part are irregular compared with hammer. Both square part and circular part are gray-scale images while hammer is a binary image. It is known that pseudo corners easily appear in irregular parts and gray-scale images. Increasing threshold $R$ of corner responding function or image binarization can remove these pseudo corners. So, the reasonable selection of threshold has a major impact on the results of parts shape recognition.

Here, supposed threshold $R \in [0,8000]$, increasing step is 500. For each threshold selected, five simulation experiments are carried out and each experiment result is recorded, which is applied to calculate average accuracy of part recognition. Fig.9 shows square part’s recognition accuracy of both the improved Harris corner detector and the original Harris corner detector. From Fig.9, the improved Harris corner detector has superiority for the biggish threshold $R$. With the threshold become larger, the number of corner gets smaller corner points’ number increasing, the matching reliability ascent. In the other words, reducing threshold, the number of corner increasing, reliability declined. In general, the improved Harris corner detector can be applied to parts shape recognition.

Parts images of different shape are applied to simulation tests. For each test case, shape recognition’s accuracy is recorded in the Table II. According to Table II, the improved Harris corner detector has a significant advantage on accuracy compared with the original Harris corner detector.

<table>
<thead>
<tr>
<th>Method</th>
<th>Improved algorithm</th>
<th>Original algorithm</th>
</tr>
</thead>
<tbody>
<tr>
<td>round</td>
<td>85%</td>
<td>72%</td>
</tr>
<tr>
<td>trapezoidal</td>
<td>87%</td>
<td>82%</td>
</tr>
<tr>
<td>rectangular</td>
<td>88%</td>
<td>84%</td>
</tr>
<tr>
<td>T-shaped</td>
<td>83%</td>
<td>70%</td>
</tr>
<tr>
<td>cross-shaped</td>
<td>80%</td>
<td>69%</td>
</tr>
</tbody>
</table>

VII. THE INNOVATION POINTS AND CONCLUDING REMARKS

This paper puts forward an improved Harris corner detector for the recognition of parts images. Based of the analysis of Harris corner detector, the improved Harris corner detector adopts a B-spline function to replace Gaussian function of Harris corner detector. In addition, this paper provides the convolution template of B-spline function. Some experiment results show that the improved Harris corner detector is effective and superior, which has better performance and efficiency than Harris corner detector.

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