Color Edge Detection by Using the Centerline Extraction Method

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Abstract—In order to obtain more complete and continuous edge information of the image, the image enhancement methods and Hessian matrix are used in the process of edge detection. Based on the gradient information of color images, the pseudo-color edges can be got by using the multi-channel edge detection. Then, enhance the edge information and remove the correlation to obtain complete edge information. The Hessian matrix is used in the last place to remove edges with redundant background texture and coarse edges so that the edge information will be more continuous and smooth. Two experiments are conducted to verify the effectiveness of the proposed method. The software is developed by using MATLAB. Experiments have confirmed that the result of proposed detection is more continuous and clearer and more details are contained. Furthermore, a good balance between the integrity and accuracy of edge detection is achieved as well.

Index Terms—color edge detection; centerline extraction; hessian matrix

I. INTRODUCTION

Edge detection, which is used in many computer vision applications, is the first fundamental and crucial step in image processing, image analysis and image understanding. The main goal of edge detection is to locate the boundaries of targets in an image. Edge detection greatly reduces the amount of insignificant information and only retains the most important information to represents the content of an image. This information is used in the subsequent target detection and recognition [1].

Color image, which contains more detailed edge information, can provide more information than gray scale image. Color edge detection has two steps, including color preprocessing and edge detection. The ways of color processing is consisted of vector-based method and color component synthesis [2-5].

Edge detection method mainly includes classical edge detection operators[6-7], mathematical morphology method[8], wavelet-based method[9], and surface fitting method[10]. There is always a contradiction between getting complete edge of the target and removing extra edge of the non-target in the traditional edge detection method.

In this case, for the purpose of obtain the complete edge information, the algorithm should not only take into account of the every component’s color information in RGB image, but also maintain the advantages of traditional edge detection methods. This paper presents a new color edge detection method. First, the pseudo-color edges of the image can be got by the gradient map of each component and combination of all the component information. The pseudo-color image should be intensified by high-frequency emphasize filter. By extracting the luminance information and converting it into a binary image is the next step. After that, de-noise and extract the four connectivity of the binary image should be done. Finally, the Hessian matrix[11, 12] will be used to extract the centerline of the edge image to obtain complete and continuous edge information.

The flow chart of the proposed algorithm contains all the key steps in the detection process, which is shown in Fig 1.
II. HELPFUL HINTS

A. Preliminary Color Image Edge Extraction

For color images, first use sobel gradient operator and the image of R, G, B components to make planar convolution to get the difference approximation of the different components under the horizontal and vertical direction. Use Fig 2 (a) to detect horizontal edges by applying the horizontal edge detection operator. Use Fig 2(b) to detect vertical edges by applying the vertical edge detection operator.

\[
\begin{pmatrix}
-1 & 0 & 1 \\
-2 & 0 & 2 \\
-1 & 0 & -1
\end{pmatrix}
\quad \begin{pmatrix}
1 & 2 & 1 \\
0 & 0 & 0 \\
-1 & -2 & -1
\end{pmatrix}
\]

(a) (b)

Figure 2. Edge detection operator

Compare the point differential value in horizontal and vertical direction after normalize the convolution result. Take each component with larger difference value as a new R, G, B value of the point, then the pseudo-color edge image is got.

Since the independence of color in ICbCr space can be exhibited better, RGB image can be transformed into ICbCr space by adopting (1).

\[
\begin{bmatrix}
0.2126 & 0.7152 & 0.0722 \\
-0.1146 & -0.3854 & 0.5 \\
0.5 & -0.4542 & -0.0458
\end{bmatrix}
\begin{bmatrix}
R \\
G \\
B
\end{bmatrix}
= 
\begin{bmatrix}
I \\
Cb \\
Cr
\end{bmatrix}
\]

Do high-frequency filtering to component I and make convolution operator with the component h and the component I. h operator is shown in (2):

\[
h = \begin{pmatrix}
-1 & 1 & -1 \\
-1 & 8 & -1 \\
-1 & -1 & -1
\end{pmatrix}
\]

The result of convolution is a matrix with the same size as I. First, calculate the difference between each pixel and the point in its 8 regional connectivity. Through this difference, the adjustment coefficient of the center point could be got. Coefficient is used to adjust each corresponding point of the matrix. Then, the matrix basis is got. Compare the point differential value in horizontal and vertical direction after normalize the convolution result. Take each component with larger difference value as a new R, G, B value of the point, then the pseudo-color edge image is got.

B. Edge Optimization

There is no need to consider the degradation of picture quality when enhancing an image. It is a process to highlight the interesting information in the image. Therefore, the edge contains much high frequency information. To highlight the edge, highlight the high frequency information of the image is a must, which requires enhancing the high frequency information. After high-frequency emphasis, the overall gray level of images is centralized. Adopting histogram equalization method to increase the overall contrast of the image, making the brightness of the image better distributed on the histogram can help to enhance the local contrast, without influence on the overall contrast.

High-pass filter belongs to filter in frequency domain. It maintains the high frequency and suppresses the low-frequency, which is a way of sharpening image. High-pass filter includes the ideal high-pass filter, Butterworth high-pass filter and Gaussian high-pass filter.

Since the high-pass filter only permits the frequency, which is greater than a certain threshold go through and forbid to pass the DC, which makes the average value of the image reduces to zero. However, DC and low frequency information are corresponding to the image's background information. Lack of background information makes the image getting darker and the visual effects become worse.

One way to solve this problem is to add an offset to high-pass filter. Combining the offset and the filter multiplied by a constant larger than 1, the high-frequency emphasize filter is formed. The constant multiplier highlights the high-frequency part and increases the range of the low frequency part. But as long as the offset is smaller than the multiplier, the impact of low-frequency enhancement will be weaker than high-frequency
enhancement. The high-frequency emphasis filter transfer function is shown in (3):

$$H_{hp}(u,v) = a + b H_{hp}(u,v)$$  \hspace{1cm} (3)$$

Wherein, the $H_{hp}(u,v)$ is a high-pass filter transfer function with $a$ is the increasing number of offset, $b$ is a constant and $b > a$, $a \geq 0$.

Histogram equalization means to use a certain algorithm to make the image histogram smooth on the whole. For the original high-contrast image, equalization would make gray-scale harmonic, and contrast decreased. For gently and whitish image, equalization can merge some gray-scale pixels to make the contrast increases.

After high frequency emphasis, the contrast of edge image is decreased and the gray-scale is centralized. Using histogram equalization can improve the global contrast and the visual effect of image.

If the size of a gray-scale image is $m*n$, $n_i$ represents the times of gray-i occurs, then the probability of the pixel with gray-i appeared is:

$$P(i) = \frac{n_i}{m*n}, \quad i \in [0, \ldots, L-1]$$  \hspace{1cm} (4)$$

$L$ is the degree of gradations, $m$ is the number of pixel rows of image, $n$ is the number of pixel columns, $P$ is the histogram of the image, normalized to $[0,1]$. Regard $C$ as a cumulative probability function corresponding to $P$, defined in (5):

$$C(i) = \sum_{j=0}^{i} P(j)$$  \hspace{1cm} (5)$$

$C$ is the normalized cumulative histogram. Create a form for the transformation of $Y = T(x)$, and produce a $Y$ for each point in the original image, the linearization of the cumulative probability function $Y$ can be carried out on all values within range. Its conversion formula as in (6):

$$Y_i = T(x_i) = c(i)$$  \hspace{1cm} (6)$$

Different levels are mapped to $[0,1]$ by $T$. In order to make these values map to the original domain, the result need to be changed as in (7):

$$Y_i' = Y_i \times (max-min) + min$$  \hspace{1cm} (7)$$

Adjust the overall gray level of the image after equalization. Calculate the average value of its gray level and the original image gray level.

In mathematics, the Hessian matrix is the square matrix of second partial derivatives of a scalar-valued function. Given the real-valued function $f(x_1, x_2, ..., x_n)$, if all partial second derivatives of $f$ exist, then the Hessian matrix of $f$ is as in (8):

$$H(i,j) = \frac{d^2f}{d(x_i)d(x_j)}$$  \hspace{1cm} (8)$$

Where $x = (x_1, x_2, ..., x_n)$, Hessian matrix that is:

$$H(f) = \begin{bmatrix}
\frac{\partial^2 f}{\partial x_1^2} & \frac{\partial^2 f}{\partial x_1 \partial x_2} & \cdots & \frac{\partial^2 f}{\partial x_1 \partial x_n} \\
\frac{\partial^2 f}{\partial x_2 \partial x_1} & \frac{\partial^2 f}{\partial x_2^2} & \cdots & \frac{\partial^2 f}{\partial x_2 \partial x_n} \\
\vdots & \vdots & \ddots & \vdots \\
\frac{\partial^2 f}{\partial x_n \partial x_1} & \frac{\partial^2 f}{\partial x_n \partial x_2} & \cdots & \frac{\partial^2 f}{\partial x_n^2}
\end{bmatrix}$$  \hspace{1cm} (9)$$

Actually, the Hessian matrix is the square matrix of second partial derivatives in the multi-variable case. It describes the change of gray level gradient in all directions.

There is a straight line on a two-dimensional plane, whose gray scale data matrix is shown in Fig. 3. Along the straight line direction on the right of the picture, which is the X direction, changes of brightness are very small so that the first order derivative and the second derivative is zero. In a direction perpendicular to the straight line on the right of the picture, which is the Y direction, the brightness changes from dark to bright, and then bright to dark.. The first order derivative of such a pulse-like edge is zero and the second derivative is less than zero and reaches minimum in the straight line, where the brightness value is highest. According to the gray-scale data matrix, calculate the Hessian matrix directly, and then calculate the two eigenvalues of the matrix and look for a straight line from different directions. It can be judged by one eigenvalue is zero and the other a negative number.

![Figure 3. The image and its first order derivative map](image)

A two-dimensional Hessian matrix form as (10).

$$H(f) = \begin{bmatrix}
\frac{\partial^2 f}{\partial x^2} & \frac{\partial^2 f}{\partial x \partial y} \\
\frac{\partial^2 f}{\partial y \partial x} & \frac{\partial^2 f}{\partial y^2}
\end{bmatrix}$$  \hspace{1cm} (10)$$

Suppose the two eigenvalues of Hessian matrix are $\lambda_1$ and $\lambda_2$. If there is a linear structure in the picture, then the two eigenvalues are bound to have a negative one. Assumes that $\lambda_1 < 0$, then the two eigenvalues must satisfy $|\lambda_1| > |\lambda_2|$, in other words, if it is a linear structure, then the ratio of the absolute values of $\lambda_1$ and $\lambda_2$ should be great.

Calculate the eigenvalue and eigenvector according to Hessian matrix to determine whether the point is on the ridge line.
In the two eigenvalues of the Hessian matrix of 2-d images, the smaller one is corresponds to the maximum gradient of the image. Assume that the smaller eigenvalue is \( \lambda_1 \), then respectively calculate the gradient of \( \lambda_1 \) along the x, y direction to get ogx, ogy. Filter the gradient matrix with the filtering operator \( W \) and process it according to (11) to (13) to get the gx and gy.

\[
W = \begin{bmatrix}
-\frac{1}{6} & 0 & -\frac{1}{6} & 0 & -\frac{1}{6} \\
0 & -\frac{1}{6} & -\frac{1}{6} & -\frac{1}{6} & 0 \\
-\frac{1}{6} & -\frac{1}{6} & 4 & -\frac{1}{6} & -\frac{1}{6} \\
0 & -\frac{1}{6} & -\frac{1}{6} & -\frac{1}{6} & 0 \\
-\frac{1}{6} & 0 & -\frac{1}{6} & 0 & -\frac{1}{6}
\end{bmatrix}
\]

Figure 4. The operator \( W \)

\[
FL1 = \sqrt{ogx^2 + ogy^2} \quad (11)
\]

FL1 still is a matrix. Calculate the average of all elements in FL1.

\[
FL2 = \frac{FL1}{E} \quad (12)
\]

\[
\begin{align*}
\text{gx} &= ogx \ast \left( \frac{0.1 \ast FL2}{FL1 + E} \right)^{0.2} \\
\text{gy} &= ogy \ast \left( \frac{0.1 \ast FL2}{FL1 + E} \right)^{0.2} 
\end{align*} \quad (13) \quad (14)
\]

The gx and gy still is matrix. Reconstruct the edge image of gx and gy by employing the Poisson rebuilding method, adjust the brightness of image and get the gradient domain reconstruction image OUT3. Use the maximum variance between clusters to obtain an appropriate threshold \( T \), and then use (15) to get the final edge image.

\[
\text{OUTIM} = \frac{1}{1 + \left( \frac{T}{\text{OUT3} + E} \right)^{20}} \quad (15)
\]

III. EXPERIMENTS & RESULTS

The two experiments conducted are used to verify the effectiveness of the proposed method. One is a comparison of detection result between the classical canny method, sobel method, the wavelet-based method and the propose method. The other is the comparison of the detection result between some latest detection methods in Ref.[14] to [18] and the proposed method.

Fig. 5 shows the results of major steps in the process of the proposed method.

![Figure 5](imageurl)

For the same original image, a comparison was made between the results of the proposed algorithm, the canny, sobel edge detection method and the wavelet based method, which are shown in Fig. 6:

![Figure 6](imageurl)

From the detection result of the letters section as shown in Fig. 6, it is obvious that the result of canny method contains more details, but excessive test occurs. The detection results of the wavelet-based and sobel method are incomplete for some edge of the target has
not been detected. But the result of the proposed algorithm contains the complete information of letters and the detailed edges of the target can be detected correctly.

The comparison of the detection results between classical algorithms and the proposed method is shown in Fig. 7.

The comparison of the detection results between the proposed algorithm and methods in paper [14] to [18] is shown in Fig. 8:

Subjective and objective evaluations are two Evaluation criteria of edge detection. To evaluate a method used in color image edge detection, both the two sides usually should be considered. A subjective evaluation criterion is to judge the result from the visual effect of edges while the objective evaluation criterion is to put forward a unified criterion from the validity and the continuity of the detection result.
To verify the effectiveness of the proposed method in this paper, the evaluation had been done from the two criteria.

For the subjective evaluation shown in Fig. 9, it is obvious that the result of the canny method is more complete, but it causes excessive test, whose result is complex and sensitive to the redundant information of background. The result of sobel method exist a relatively serious undetected phenomenon for the edge of the target is incomplete. The result of the wavelet based method is unstable and this method is only suitable for some images. Besides, most of the edge cannot be detected. The result of the method proposed in paper [14] has many redundancy information and background texture information. The result of the method in paper [15] has a coarse edge, which is not smooth enough. The result of the method in paper [16] shows many breakpoints and the continuity is poor. The result of the method in paper [17] exist undetected area and the edge is also not smooth enough. The result of the method in paper [18] is unclearly and the continuity is poor.

For the subjective evaluation, it is easily to confirm that the result of the proposed method is more complete, continuous and smooth, and insensitive to background redundancy, the effect is stable based on the comparison.

For the objective evaluation, the evaluation criteria put forwarded by paper [19] is used in this paper. This criteria means to use the number of the points along the edge, the number of 4-connectivity and 8-connectivity, and the connected component ratio as standards to objectively compare the detection result of different methods. The result was shown in table 1:

<table>
<thead>
<tr>
<th>TABLE I. DETECTION RESULT OF THE VARIOUS METHODS</th>
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<tbody>
<tr>
<td>Baboon</td>
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</table>
In table 1, X stand for the number of the point along the edge, Y and Z respectively stand for the number of 4-connected and 8-connected region. Y / X and Z / X, respectively represent the percentage of the number of 4-connectivity and 8-connectivity in total edge points. The smaller the percentage, the better the continuity.

Under the same evaluation criteria, the detection results of the proposed method and eight other methods were shown in table 1. Through the data in table, it is easy to find that the two indicators Y/X and Z/X in proposed method are always the minimum. It shows that the continuity of the detection result of the proposed method is better than the others. So a conclusion can be reached that both from the subjective and objective criteria to evaluate, the result of the proposed edge detection is more complete, smooth, and continuous.

IV. CONCLUSIONS

This article improved the algorithm based on the color space and proposed a new method for edge detection with the combination of edge optimization. Experimental results have confirmed that this proposed color edge detection method can provide more reasonable results compared with several other algorithms. It can improve integrity and continuity, lower undetected rate and possess good adaptability.

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