

# GA-based Global Path Planning for Mobile Robot Employing A\* Algorithm

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**Abstract**—Global path planning for mobile robot using genetic algorithm and A\* algorithm is investigated in this paper. The proposed algorithm includes three steps: the MAKLINK graph theory is adopted to establish the free space model of mobile robots firstly, then Dijkstra algorithm is utilized for finding a feasible collision-free path, finally the global optimal path of mobile robots is obtained based on the hybrid algorithm of A\* algorithm and genetic algorithm. Experimental results indicate that the proposed algorithm has better performance than Dijkstra algorithm in term of both solution quality and computational time, and thus it is a viable approach to mobile robot global path planning.

**Index Terms**—Dijkstra algorithm, Global path-planning, Genetic Algorithm, A\* Algorithm.

## I. INTRODUCTION

The global optimal path planning as the second factor for mobile robots have been a hotspot research area for many years, and several optimization methods such as potential field method [1-3], visibility graph method [2], grid method [3-5], modified simulated annealing algorithm [9] and straight line path planning [10] have been developed to solve this problem. For the grid method, the main problem is how to determine the size of grid, which has great influence on both the representation precision for obstacles and the planned path. In recent years, many intelligent algorithms were applied to the path planning for mobile robots, such as fuzzy logic and reinforcement learning [6], neural network [7], genetic algorithm [8], and so on.

## II. GENETIC ALGORITHM TECHNIQUE FOR GLOBAL ROBOT PATH-PLANNING

The path-planning problem is usually defined as follows [14]: "Given a robot and a description of an environment, plan a path between two specific locations. The path must be collision-free (feasible) and satisfy certain optimization criteria." The problem emerges after all the viewpoints are generated for a given part: find the minimum-time movement of the eye-in-hand robot to visit all the viewpoints. It is a reasonable assumption that the camera completely stops at each viewpoint and the

time to execute an inspection at all viewpoints is the same, i.e., all equal to a constant time.

Mainly, two factors determine the traverse time: (i) the trajectory, or time history of joint positions, velocities, accelerations, and torques, between each pair of viewpoints; (ii) the order to visit all the viewpoints, global path planning. Obviously if the number of viewpoints is big, the ordering of the viewpoints will be the dominant factor; therefore, both of the factors would be considered in this paper.

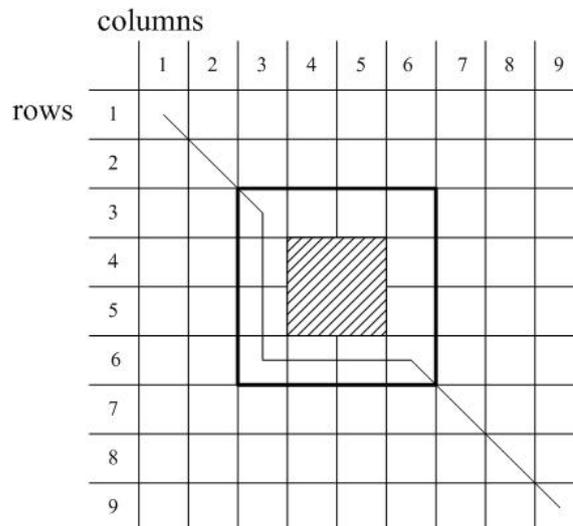


Figure 1. Path-planning example for local obstacle avoidance, applied on a subsection of the search space.

Global path planning requires the environment to be completely known and the terrain should be static. In this approach the algorithm generates a complete path from the start point to the destination point before the robot starts its motion. On the other hand, local path planning means that path planning is done while the robot is moving; in other words, the algorithm is capable of producing a new path in response to environmental changes. Assuming that there are no obstacles in the navigation area, the shortest path between the start point and the end point is a straight line. The robot will proceed along this path until an obstacle is detected. At this point,

our path-planning algorithm is utilized to find a feasible path around the obstacle. After avoiding the obstacle, the robot continues to navigate toward the endpoint along a straight line. An example of local path planning is shown in Figure 1.

Genetic algorithms [15,26-28] are a class of adaptive methods that can be used to solve search and optimization problems involving large search spaces. The search is performed using the idea of simulated evolution (survival of

the fittest). These algorithms maintain and manipulate “generations” of potential solutions or “populations”. With each generation, the best solutions (as determined by a problem specific fitness function) are genetically manipulated to form the solution set for the following generation. As in nature, solutions are combined (via crossover) and/or undergo random mutation.

Robot path-planning is part of a larger class of problems pertaining to scheduling and routing, and is known to be NP-hard(NP-complete) [15]. Thus, a heuristic optimization approach is recommended as shown by Hwang [16]. One of these approaches is the use of genetic algorithms. A genetic algorithm (GA) is an evolutionary problem solving method, where the solution to a problem evolves after a number of iterations. A proposed solution with the GA method to the path-planning problem is the best feasible path among the pool of all possible solutions.

There have been several contemporary applications of genetic algorithms to the robot navigation problem. One approach is to combine fuzzy logic with genetic algorithms[17,18,19]. In this approach, the genotype structure represents fuzzy rules that guide the robot navigation, so the genetic algorithm evolves the best set of rules. While this approach can produce a feasible path through an uncertain environment, the genotype structure becomes very complex, as it needs to represent a variety of fuzzy rules. A complex genotype structure can take a long time to process in a genetic algorithm, which affects the real-time performance of the robot during navigation.

Another approach is to use genotype structures that represent local distance and direction, as opposed to representing an entire path [20,21,22,23]. While these are simple to process and allow for faster real-time performance, the local viewpoint of these methods may not allow the robot to reach its target. Some methods have relatively simple genotype structures that can represent feasible paths, but require complex decoders and fitness functions [24, 14, 25].

Thus, our research has focused on improving the genetic algorithm performance.

### III. SPACE MODEL OF MOBILE ROBOT’S WORKING ENVIRONMENT

A working environment of a mobile robot is illustrated as shown in figure 1. Between the given starting point S and goal point T, an area with 500×500 cm<sup>2</sup> is enclosed, robotic diameter is about 36cm,so the motion region could be divided into 15 × 15 regional grids . The free space for the mobile robot in the environment with obstacles consists of some polygonal areas. For each of

the six obstacles, the black polygon denotes its original size, and the white margin denotes its expanded part. A black part plus its white margin constitute a so-called “grown obstacle”. In Figure 1, the symbols A1, A2, ... and A15 denote respectively the vertices of these grown obstacles.The (x, y) coordinates of the starting point S and the goal T are ( 1, 1 ) and ( 15, 15 ), respectively.

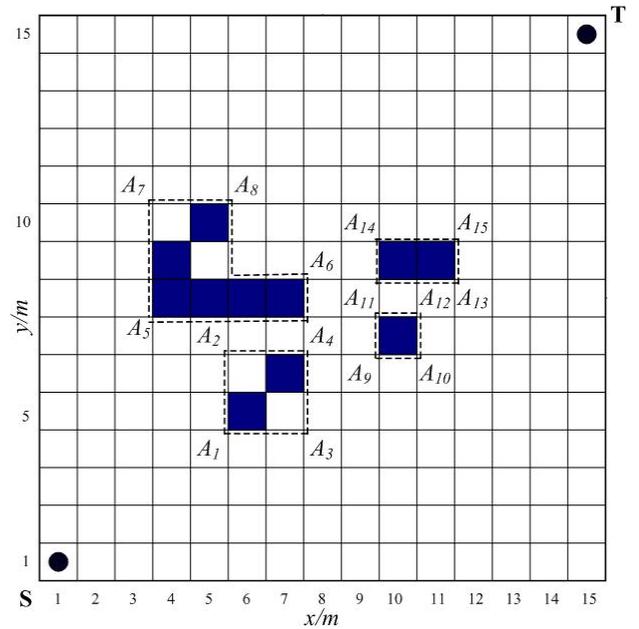


Figure 2. Working environment and its regional grids

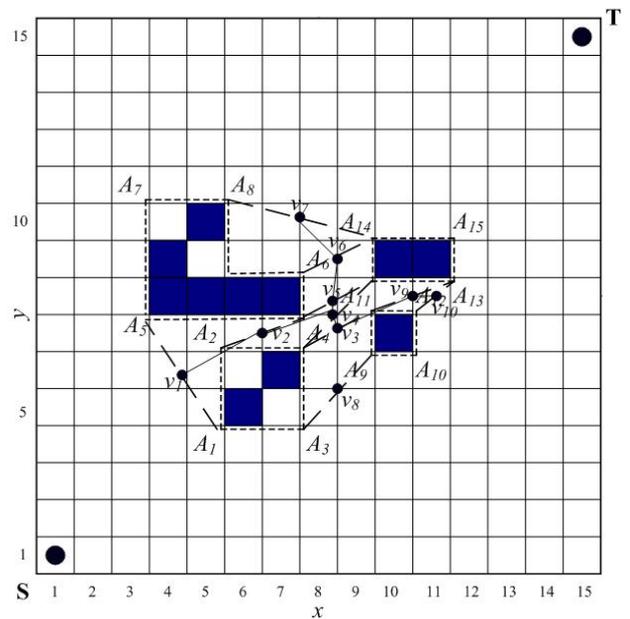


Figure 3. Network graph for free motion of mobile robot.

Assuming that the symbol l denoted the total number of the free MAKLINK lines on a MAKLINK graph, these middle points of these free MAKLINK lines were denoted respectively by v1,v2, ..., vl. If each pair of the middle points on two adjacent free MAKLINK lines were connected together, a network graph could be formed, which gave the possible paths for the free motion of the mobile robot. In Figure 2, the starting point S and the

goal point T were also denoted by  $v_0$ , and  $v_{l+1}$ , respectively. Figure 2 was an undirected graph, we used  $G(V, E)$  to denote it, where  $V=\{v_0, v_1, v_2, \dots, v_l, v_{l+1}\}$  was the set which consisted of S, T, and the middle points of all the free MAKLINK lines and E was the set which consisted of the lines connecting each pair of the middle points on two adjacent free MAKLINK lines, the lines connecting S (or T) and the middle points on the free MAKLINK lines adjacent to S (or T). Using the undirected graph  $G(V,E)$  as the free space model, the global optimal path planning for the mobile robot could be solved by finding the shortest path between the given starting point S and goal point T on the graph  $G(V, E)$ .

#### IV. FINDING FEASIBLE PATH USING DIJKSTRA ALGORITHM

In this section, to obtain a feasible path, we adopt Dijkstra algorithm [14] to find it between the given starting point S and the goal T on the graph  $G(V, E)$  and find out all the free MAKLINK lines at which the path intersects at  $v_i$  ( $i=1,2,\dots,l$ ), then connect the obstacle vertexes corresponding to those free MAKLINK lines, and S and T to be a closed free-space. This way, we obtained a sub-search-space where the global optimal path inside.

Before using the Dijkstra algorithm, it is necessary to define the adjacency matrix with weights for the network graph  $G(V, E)$ , which is the basis for computing the shortest path on  $G(V, E)$ . Each element of the matrix represents the length of the straight line between two adjacent path nodes on  $G(V, E)$ , where a path node means the intersection of the moving path for the mobile robot and a free MAKLINK line. And each element of the adjacency matrix is defined as follows.

$$adjlist[i][j]=\begin{cases} length(v_i, v_j), & if\ edge(v_i, v_j) \in E \\ \infty, & other \end{cases}$$

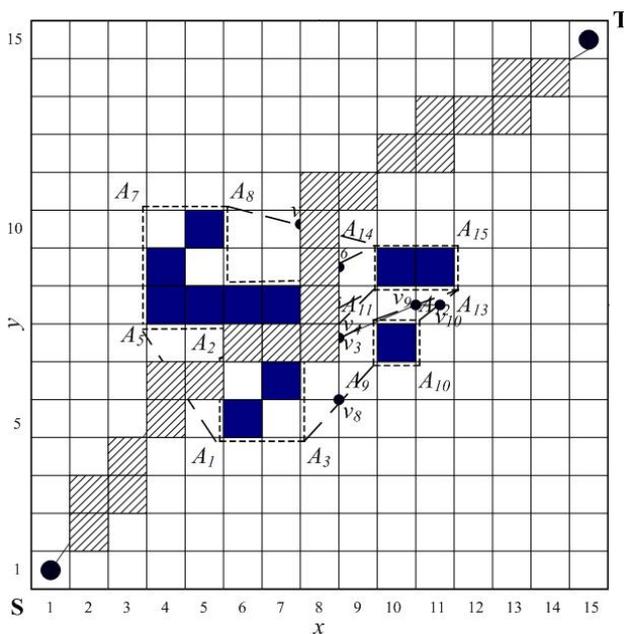


Figure 4. Paths generated by Dijkstra algorithm.

Where  $adjlist[i][j]$  is the element corresponding to the  $i$ th row and the  $j$ th column of the matrix;  $length(v_i, v_j)$  is the length of the straight line between the points  $v_i$  and  $v_j$ ;  $i$  and  $j=0, 1, 2, \dots, l, l+1$ .

For the example given in Figure 1, by using Dijkstra algorithm, the path is obtained as:

$S \rightarrow v_1 \rightarrow v_2 \rightarrow v_4 \rightarrow v_5 \rightarrow v_6 \rightarrow v_7 \rightarrow T$ , and the path of the mobile robot is shown in Figure 3. The path of the robot is about 24 grids.

#### V. GLOBAL OPTIMAL PATH PLANNING BASED GA ON GA AND A\* ALGORITHM

##### 1) Genetic Algorithm

GA optimizers classified as global optimizers are robust and stochastic search methods modeled on principles and concepts of natural selection and evolution [12]. A basic task of GA optimizer must be performed is encoding the solution parameter as genes. The convergence speed largely depends on the encoding method. Binary encoding has some disadvantages when optimized variable dimension is high. Encoding with real numbers is proposed in this paper, which could improve precision of the solution. The value of the genes is denoted by some real number, the length of code depends on the number of decision-making individuals. Before the decision is made, the best individuals of current generation are chosen to contrast against those of the pre-generation, and the better are kept back for the next comparison without any operation of GAs [13].

##### 2) A\* algorithm

A\* algorithms do the evaluation to each node, in order to find a the most promising node. The evaluation function  $f(n)=g(n)+ h(n)$  is introduced into the algorithm.  $g(n)$  is the cost value of the shortest path from an initial node to the current node,  $h(n)$  is a cost evaluation of the optimal path from node  $n$  to the goal [11].

##### 3) Global Optimal Path Planning

The algorithm based on GA and A\* algorithm is described as follows:

###### Step1. Path Eoder Mode

Initialize starting point S:  $P_0(x_0, y_0), x_0=1, y_0=1$ ; and initialize goal point T:  $P_n(x_n, y_n), x_n=15, y_n=15$ . The obstacles could be indicated as  $OR_i (i=1, 2, \dots, q)$ , so there is a finite set  $\Phi, \Phi= \{OR_1, OR_2, \dots, OR_q\}$

The intermediate nodes need 2 to meet 3 points as follow:

- i The nodes should be located outside the obstacle.
- ii The nodes should be located in the planning space.
- iii The paths should not intersect the obstacles.

So the initial population is the point to point paths.

###### Step 2. The Fitness Function

The Fitness Function is the important factor to influence the astringency and stability of Genetic algorithm. The nodes has met the 3 needs in the globe path planning during the selection, the robotic length of the path is still in the consideration when determining the function

The evaluation function  $f^*$  is the core design in A\* algorithm,

$$f^*(i) = g(i) + h^*(i)$$

$g(i)$  is the measurement of the actual cost from source point to the goal,  $h^*(i)$  is the evaluation of minimum cost from node  $P_i$  to the goal.

When the valuation functions is the shortest path from source to the goal, and the network could be viewed as a planar network,  $h^*(i)$  of A\* algorithm would be Euclidean distance from  $P_i$  to the goal.

Based on A\* algorithm, set the fitness fuction as  $f=A+B$

$$A = \alpha \sum_{i=1}^n (h^*(i) / g(i));$$

$$B = \beta (\sum_{i=1}^n (ORi(k))^2 + \dots + \sum_{i=1}^n (ORq(k))^2)$$

A is to make sure the path is shortest from source to the goal,  $\alpha \in [100,300]$ , in this paper  $\alpha = 200$ , B is to make sure the path is safe,  $\beta \in [0.1,0.5]$ .

$$ORi(k) = \min \{0, ((xk - xi)^2 + (yk - yi)^2 - r^2)\},$$

$$i = 1, 2, \dots, q$$

Step3. Genetic Operator

(1) Selection Operator

Force the individual reproduce to the next generation on the direct proportion according to the fitness.

(2) Crossover Operator

Use the single-point crossover. First, assume the crossover probability  $p_c$ , match the individuals randomly, then generate a random number  $r(r \in [0,1])$  for individual, if  $r < p_c$ , crossover operate the random gene of individual.

(3) Mutation Operator

Mutation is to add some random vibration in the genes of the population, the mutation probability  $p_m$  is around 0.001~0.100.

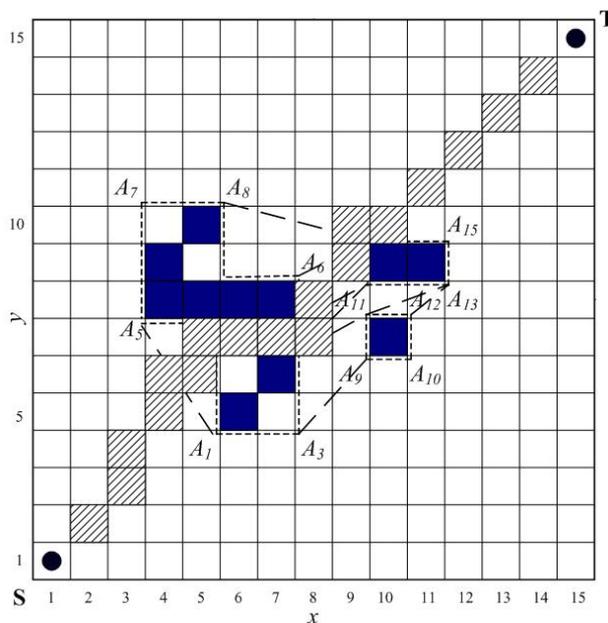


Figure 5. Computer simulation

### 1) Simulation Results

We carry out a computer simulation experiment for the example illustrated in figure 1 using this paper method. The simulation parameters are set as: M=30 (population size),  $P_c=0.7$ (initial crossover probability),  $P_m=0.05$  (initial mutation probability), The result of simulation experiment is shown in Figure 4.

In figure 4, the shadow part denotes the global optimal path with the length of 20, which obtained by this paper method.

TABLE I.  
COMPARISON OF THREE ALGORITHMS ON GLOBAL OPTIMAL PATH PLANNING

Algorithm	Dijkstra	This paper
Performance		
LENGTH OF PATH(GRIDS)	24	20
EXECUTION TIME (S)	11.857	3.142

To proof the proposed method to be correct, the comparison results with two methods (Dijkstra algorithm, and this paper) on the global optimal path planning problem as shown in figure 1 are given as seen Table 1.

In Table 1, Dijkstra algorithm expends 11.857 s to find the global optimal one with the length of 24 grids; this paper method expends 3.142 s to find the global optimal path one with the length of 20 grids. From the above table, we can see that, compared with the method in dijkstra algorithm, the global optimal path obtained in this paper is shorter and require less time.

### VI. CONCLUSION

In this paper, a method of global optimal path planning for mobile robots based on GA and A\* algorithm is proposed to solve the problems existing in dijkstra algorithm. The Dijkstra algorithm is used to find a feasible path in the graph of mobile robot environment. A\* algorithm was used to overcome its disadvantage of poor local optimizing. The simulation results show that the proposed method is correct, its search speed is faster than Dijkstra algorithm, and its search quality is better than that of recently reported methods.

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