Community Discovery Algorithm Based on Ant Colony and Signal Transfer

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Abstract: With continuous emergence of social network platforms, the research of complex network has become a hot field. Complex networks have an obvious feature of community structure, which could be used to study other network characteristics. However, how to better research community structure also becomes a problem that scholars have been exploring. Detecting community structure contributes to analyzing networks to further discover its implicit patterns. This paper proposes a community discovery algorithm that combines foraging model of ant colony algorithm and signal transmission mechanism to detect overlapping communities. Ants will release pheromones to guide other partners to find the optimal solution, meanwhile pheromones will evaporate at a certain probability. On the other hand, some signals will be lost during transmission. We apply the mechanism of signal loss to process of pheromone evaporation, and consider the similarity between ants to construct ant transfer matrix. Through above two aspects, ant colonies will choose a better walking strategy. In this way, our algorithm can get better division results by adopting above strategy. What’s more, our experiment results indicate that our proposed algorithm could obtain a higher modular value $Q$ and NMI (Normalized Mutual Information) value, which shows very excellent performance in discovering overlapping communities.

Key words: Complex network, community detection, ant colony algorithm, signal transfer, walking strategy.

1. Introduction

Nowadays, virtual communities and social platforms have gradually penetrated into our lives and actual production [1]. In this context, how to better analyze social network structure has become a hot topic of current research. Community discovery is a basic task of social network analysis, which is used to study various network phenomena [2]. It is well known that complex networks have common properties: scale-free property, small world property [3], community structure characteristics [4], [5].

Community discovery is a division of real social network, which has become an important subject of social science, physical science, biological science and computer science [6]. In 2005, Palla proposed a CPM algorithm for mining overlapping communities. Subsequently, Palla designed a software CFinder [7]. After that, COPRA algorithm is proposed by Steve Gregory [8], [9]. Shen [10] et al proposed EAGLE algorithm, and Fuzzy clustering method was also applied to overlapping community discovery [11]. Reza [12] proposed a SATOCI algorithm based on intelligent swarm. As in [13], ant colony algorithm is proposed to detect overlapping community structure through ant colony foraging model.

Ant colony algorithm is a probabilistic algorithm for finding the optimal path [14], [15]. The ant colony
The system was first proposed by Italy scholars Dorigo, Maniezzo and others in the 1990s [16]. Individuals in social networks communicate information with each other to form communities, and individuals in the same community have similar information [17]. References [18], [19] have proposed signal transmission methods. This paper combines the idea of signal transfer loss and ant colonies foraging model to detect overlapping communities. Pheromone released by ant colonies will evaporate at a certain probability, which is similar to the phenomenon that some signal will lose in the transmission process. We apply signal transfer into ant colonies foraging model to optimize our algorithm. And here we consider similarity between ants as another factor to construct transition matrix. In this way, we could get better division results by the optimal strategy.

2. Theory Analysis

2.1. Ant Colony Foraging Model Analysis

In the process of searching food, ant colonies will release a substance called pheromones. Ants in ant colonies are sensitive to pheromones, and they walk along higher concentrations of pheromones. It's common that ant colonies are not only affected by pheromones, but also by obstacles and other ants. Ant colony algorithm adopts the positive feedback mechanism, so that search process converges continuously and finally approaches the optimal solution.

As shown in Fig. 1, there are a group of ants, assuming that $A$ is an ant nest, and $F$ is a food source. Under normal conditions (Fig. 1 (a)), ants at $A$ will walk along straight lines to find food. If there is an obstacle between $A$ and $F$ (Fig. 1 (b)), then ants will make a decision at $B$ point, left or right. At first, the probability that ants walk in two directions is the same because there are no pheromones left by other ants. As time goes on, ants in front will leave pheromones on the road and ants in the back will choose strategy by these pheromones. In this way, more and more ant colonies walk along the shortest path, and at the same time, pheromone on this path becomes more and more dense.

![Fig. 1. Ant colony foraging model](image)

2.2. Signal Transmission Theory Analysis

According to signal transduction mechanism, we suppose that a network with $n$ nodes is $V = \{V_1, V_2, \ldots, V_n\}$. Here for any node $V_j \in V$ that has the ability to send, receive and record signals. Each node only transmits signals to itself and neighbor nodes, and signals that receive from others can be transmitted in turn. The specific signal transfer process is shown in Fig. 2 (a) below:

![Fig. 2. Signal transfer process](image)

Obviously, node 1 is selected randomly and its signal value is initialized 1, whereas remaining nodes are 0 in Fig. 2 (a) (1); In Fig. 2(a) (2), node 1 passes signal value to its neighbor nodes, so signal value of all
nodes is 1; Similarly, each node passes signal value to neighbor nodes and itself respectively in Fig. 2 (a) (3) (4).

The above procedure is expressed as follows:

\[ V(T) = (A + I)^T \tag{1} \]

Here, \( A \) represents adjacency matrix, \( T \) indicates iteration number and \( T=\{1, 2, 3, \ldots \} \), \( I \) is unit matrix.

As shown in Fig. 2 (b), we could get the vector \((1,1,1,1,1,1)\) by \( V(1) = (A + I) \) where \( T=1 \); the vector is \((6,4,4,4,3,3)\) by \( V(2) = (A + I)^2 \) where \( T=2 \); and the final vector is \((24,18,18,12,12,12)\) by \( V(3) = (A + I)^3 \) where \( T=3 \). This final vector represents impact of initial node 1 on the entire network after the end of three signal transmission.

Let we define probability that node \( j \) receive signals of node \( i \) and its formula is as follows:

\[ p(j, i) = \frac{d_i}{n-1} \tag{2} \]

where \( d_i \) stands for degree of node \( i \) and \( n \) denotes the number of nodes. The adjacency matrix of the network is \( A = \{A_1, A_2, \ldots, A_n\} \), \( A_i = \{a_{i1}, a_{i2}, \ldots, a_{in}\} \) \((i=1,2,\ldots,n)\). If there exists edge between \( i \) and \( j \), \( a_{ij}=1 \). Otherwise \( a_{ij}=0 \) when \( i=j \). Meanwhile, signal loss matrix is defined as \( P = \{P_1, P_2, \ldots, P_n\} \), \((i=1,2,\ldots,n)\). According to (2), each element in the loss matrix is defined as \( P_i = p(j, i)A_i \). Thus final matrix after transmission in the case of signal loss is as follows:

\[ V = p^T A + p^{T-1} + \ldots + I \tag{3} \]

By (3), a set of nodes after passing \( T \) times is obtained: \( V' = \{V'_1, V'_2, \ldots, V'_n\} \) , where \( V'_i = \{v'_{i1}, v'_{i2}, \ldots, v'_{im}\} \). In order to further obtain its relative influence quantity, we normalize it as \( F_i = \{f_{i1}, f_{i2}, \ldots, f_{in}\} \), where \( f_{ij} = \frac{v'_{ij}}{\sqrt{\sum_{k=1}^{n} (v'_{ik})^2}} \). \( F_i \) represents the impact of node \( i \) on entire network, so we convert topology map into \( n \)-dimensional vectors. Fig. 2(b) shows the final result in case of signal loss:

Fig. 2. Signal transduction process.
2.3. Improved Ant Colony Walking Strategy

Here an ant colony guide model is proposed to measure influence of ant colonies, which can be described from two aspects: ant neighbours and their edge relation. The formula for measuring similarity between ants is as follows:

$$s_{ij} = \alpha \frac{|N(i) \cap N(j)|}{|N(i) \cup N(j)|} + (1-\alpha) \frac{|E(N(i)) \cap E(N(j))|}{|E(N(i)) \cup E(N(j))|}$$  \hspace{1cm} (4)

Here first part describes neighbor nodes, $N(i)$ and $N(j)$ represent neighbor nodes of $i$ and $j$ respectively. $|N(i) \cap N(j)|$ represents the number of common neighbors for node $i$ and $j$. $|N(i) \cup N(j)|$ denotes the number of all neighbors of $i$ and $j$. In second section, $E(N(i))$ and $E(N(j))$ represent sets of neighbors' edges of $i$ and $j$ respectively. $|E(N(i)) \cap E(N(j))|$ stands for the number of common edges between neighbors of $i$ and $j$, and $|E(N(i)) \cup E(N(j)) \cup E(i,j)|$ is the number of all edges in the graph.

Next, we construct ant colonies transition matrix by combining pheromone and similar guidance. Walking transition matrix is defined here $M = [m(i,j)]_{n \times n}$, where element $m(i,j)$ is obtained by following two cases:

1. $j \in N(i)$;
   - Under this case, elements are calculated according to the following formula:
     $$m(i,j) = \frac{(f_{ij}^{+})(s_{ij}^{\mu})}{\sum_{o \in N(i)}(f_{ij}^{+})(s_{ij}^{\mu})}$$  \hspace{1cm} (5)

2. $j$ is not exist in $N(i)$;
   - Under this case, element $m(i,j)=0$.

In formula (5), $f_{ij}$ stands for pheromone and is calculated by (3). $s_{ij}$ is similarity between ants by (4). Here $\lambda$ and $\mu$ represent weights of pheromone and similar guidance, and these two values usually determine the search performance of algorithm.

3. Algorithm Description

Overlapping community detection algorithm (Ant-Signal Algorithm) based on ant colony and signal transmission is proposed in this paper, including following processes:

<table>
<thead>
<tr>
<th>Table 1. Ant-Signal Algorithm Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input:</strong> Initialized ant colonies: $G=(V,E), T, n, f, \alpha$;</td>
</tr>
<tr>
<td><strong>Output:</strong> Overlapping community results: $C$</td>
</tr>
<tr>
<td>1. Ant colony location initialization;</td>
</tr>
<tr>
<td>2. Calculate colony pheromones according to formula (3);</td>
</tr>
<tr>
<td>3. Calculate similarity of similar ants according to formula (4);</td>
</tr>
<tr>
<td>4. Construct ant colony transfer matrix according to formula (5);</td>
</tr>
<tr>
<td>5. Start for $t=1$ to $T$</td>
</tr>
<tr>
<td>for $i=1$ to $n$</td>
</tr>
<tr>
<td>Each ant chooses the walking strategy according to the transfer matrix;</td>
</tr>
<tr>
<td>Update pheromone and similarity on edge;</td>
</tr>
<tr>
<td>End for</td>
</tr>
<tr>
<td>6. Get overlapping community results.</td>
</tr>
</tbody>
</table>
4. Experimental Design

4.1. Datasets and Evaluation Criterion

Our experimental datasets include two real data sets and a simulated data set. And these two real datasets are Zachary karate club and dolphin network. Zachary’s Karate Club [20] data set is one of small community structure networks commonly used in complex networks. Dolphin Social Networks [21] is more complex than Zachary network, including 62 nodes and 159 edges. Artificial analog network LFR [22] is an extension of GN networks.

Here we adopt modular $Q_{ov}$ value [23] as criterion to evaluate performance of our algorithm. For networks generated by LFR simulations, we adopt extended NMI (Normalized Mutual Information) to measure the accuracy of algorithms for mining communities.

4.2. Results and Analysis

In order to validate the overlapping community detection algorithm based on ant colonies and signal (AntSigA), we compare our proposed algorithm with classic COPRA algorithm and CPM algorithm.

The following Table 2 shows basic description of Karate Club data sets and Dolphin data sets:

<table>
<thead>
<tr>
<th>DataSets</th>
<th>Vertex</th>
<th>Edge</th>
<th>Average k Value</th>
<th>Community</th>
</tr>
</thead>
<tbody>
<tr>
<td>Karate</td>
<td>34</td>
<td>78</td>
<td>4.5</td>
<td>2</td>
</tr>
<tr>
<td>Dolphins</td>
<td>62</td>
<td>159</td>
<td>5.1</td>
<td>2</td>
</tr>
</tbody>
</table>

Through above experiments, we obtain modular values of three algorithms on two real datasets. Results are shown in Table 3:

<table>
<thead>
<tr>
<th>DataSets</th>
<th>AntSigA</th>
<th>COPRA</th>
<th>CPM</th>
</tr>
</thead>
<tbody>
<tr>
<td>Karate</td>
<td>0.68</td>
<td>0.47</td>
<td>0.48</td>
</tr>
<tr>
<td>Dolphins</td>
<td>0.68</td>
<td>0.655</td>
<td>0.62</td>
</tr>
</tbody>
</table>

Table 3 describes $Q_{ov}$ value results of AntSigA algorithm and other two algorithms in real datasets. In order to make a clearer comparison of results, we draw above results into Fig. 3:

![Fig. 3. Results contrast.](image)

It’s clearly that $Q_{ov}$ value of AntSigA algorithm is higher than that of COPRA algorithm and CPM algorithm. Next, we study the performance of three algorithms on LFR datasets. By setting different parameters on the LFR, we obtain three simulated networks. Their specific parameters are listed below:
Table 4. Parameter Setting in LFR

<table>
<thead>
<tr>
<th>DataSets</th>
<th>N</th>
<th>μ</th>
<th>Community Size</th>
<th>O_n</th>
<th>O_m</th>
</tr>
</thead>
<tbody>
<tr>
<td>LFR1</td>
<td>100</td>
<td>0.1</td>
<td>2,10</td>
<td>10</td>
<td>2,3,4,5</td>
</tr>
<tr>
<td>LFR2</td>
<td>100</td>
<td>0.3</td>
<td>2,10</td>
<td>10</td>
<td>2,3,4,5</td>
</tr>
<tr>
<td>LFR3</td>
<td>500</td>
<td>0.1</td>
<td>2,10</td>
<td>50</td>
<td>2,3,4,5</td>
</tr>
</tbody>
</table>

Here $N$ is the number of nodes; $\mu$ is a mixed parameter that represents connection rate of a node with other nodes in same community, and here $\mu$ is setted to 0.1 or 0.3; The smallest size of community is 2 and the largest is 10; $O_n$ stands for number of overlapping nodes in a network; $O_m$ stands for the number of communities that overlapping nodes belong to, here are 2, 3, 4, 5.

On the whole, NMI value of AntSigA algorithm is higher than other two algorithms' NMI values by combining with Fig. 4, and the performance of our algorithm is also relatively excellent. Separately, Fig. 4 where in LFR1 and LFR3 are case of $\mu$=0.1, and NMI decreases as the number of communities increases where overlapping nodes exist in. In Fig. 4 where in LFR3, the NMI value of AntSigA algorithm is similar to value of CPM when $O_m$=2. In other words, CPM will be better suitable for discovering community structures when $O_m$ is small, but its performance will gradually decrease as $O_m$ grows. Additionally, NMI values of three algorithms are higher when the ambiguity is 0.1 in LFR1, LFR2 where $\mu$=0.1, $\mu$=0.3.

5. Conclusion

This paper analyzes and summarizes existing community detection algorithms, and proposes an overlapping community detection algorithm based on ant colonies and signal transfer for overlapping community partition. Firstly, the ant foraging model is analyzed. In process of walking, ants will release pheromones to guide other partners to select the optimal path. However, these pheromones will evaporate at a certain probability, which will affect the change of selection strategy. Secondly, we analyze the mechanism of signal transmission: some signals will be lost during transmission. Based on above two aspects, this paper applies mechanism of signal loss to the process of pheromone evaporation. Thus, we further construct the walking transition matrix, and ants will reach the destination through guidance of the selected strategy. Finally, overlapping community division results are obtained by above process.

The following work focuses on solving two problems. How to apply our algorithm to large-scale networks needs to be studied. At the same time, dynamic community discovery has a wide range of applications, how to divide dynamic community is also an important problem.

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